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Exercise

Find the DFS spanning trees starting with E and H.



What is the order of each traversal.

Breadth-First Search (1) From a start/root vertex, explore the next level of the spanning tree before exploring the following level. Example: BFS on the following graph starting with A. We will break ties by choosing edges that connect to vertices in alphabetic order. Prof. Adam J. Aviv (GW) Lec 23: Graphs and Trees V 13 / 21

Breadth-First Search (2)

Starting with A (at level 0), the next level of the tree would include B and C.

At B and C, the next level (level 2), would include E, F, G, D, and H





Ties are broken by Alphabetic order. We first visit B and then C, left to right across level 1 in the spanning tree.

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Breadth-First Search (5)

We've tracked the spanning tree during the traversal.

The traversal order is now a *level-order traversal* of the spanning tree, where each level is enumerated left-to-right, top-to-bottom.

$$A, B, C, E, F, D, G, H, I, I, K, J, M, L, O, N$$

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Shortest Path and BFS

The spanning tree for BFS is also a minimum spanning tree, which defines the smallest distance (in terms of number of edges in the path) between the root and other vertices.



For example, the distance between A and J is 4 "hops" as j is on level 4 of the tree.

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Why does BFS define the minimum spanning tree?

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Minimum Spanning Trees with Weighted Edges

If a graph have weighted edges, a minimum spanning tree (MST) is the



For example, a weighted graph with distances between cities in the USA, the (MST) from Washington would define the shortest path via other

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Solving shortest path problems

Solutions for the shortest path in a graph (or network) is extremely important to computer science. There are number of seminal algorithms.

- Dijkstra's Algorithm
- Prim's Algorithm
- Kruskal's Algorithm

The book discusses each of these in detail, but they will likely be covered in your Algorithms or Computer Network classes.

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